

Adv. Algebra 2 – Concept Quiz

Form B

Name: *key

Date: _____ Period: _____

21. Graphs of Rational Functions

a) Find the characteristics listed below of the function $f(x) = \frac{x^2 - 11x + 28}{x - 6}$.

a. Vertical Asymptote $x = 6$

b. End Behavior $y = x - 5$

c. x-intercept(s) $(7, 0)$ $(4, 0)$

d. y-intercept $(0, -\frac{14}{3})$

$$\frac{(x-7)(x-4)}{(x-6)}$$

$$6 \overline{) \begin{array}{r} 1 \quad -11 \quad 28 \\ \underline{6 } \\ 1 \quad -5 \quad 28 \\ \underline{6 } \\ 1 \quad -5 \quad 28 \end{array}}$$

$$x - 5 + \frac{-2}{x-6}$$

$$\frac{28}{-6} = -\frac{14}{3}$$

b) As x gets larger and larger in the positive and negative direction, the graph of $g(x) = \frac{4x-9}{x-3}$ approaches the line $y = 4$. Explain why this is end behavior of $g(x)$.

22. Solving Rational Equations

a) Find all values of x that make the equation true.

$$5 + \frac{4}{x^2 + 2x} = \frac{x}{x+2}$$

$$\frac{(x^2 + 2x)}{(x^2 + 2x)} \cdot 5 + \frac{4}{x^2 + 2x} = \frac{x}{x+2}$$

$$\frac{5x^2 + 10x}{x^2 + 2x} + \frac{4}{x^2 + 2x} = \frac{x}{x+2}$$

$$\frac{5x^2 + 10x + 4}{(x+2) \cdot x} = \frac{x}{x+2} \cdot \frac{(x+2) \cdot x}{(x+2) \cdot x}$$

$$5x^2 + 10x + 4 = x^2$$

$$4x^2 + 10x + 4 = 0$$

$$2x^2 + 5x + 2 = 0$$

$$2x^2 + 4x + 1x + 2 = 0$$

$$2x(x+2) + 1(x+2) = 0$$

$$(x+2)(2x+1) = 0$$

$$x = -2, -\frac{1}{2}$$

$x = -\frac{1}{2}$ (circled)

b) How can extraneous solutions arise in the process of solving an equation?

23. Multiply and Divide Rational Expressions

$$\frac{2x^2 - 13x + 15}{14x^3 - 21x^2} \div \frac{x^2 - 25}{14x^2 + 70x}$$

$\frac{2}{x}$ (circled)

24. Adding and Subtracting Rational Expressions

$$\frac{7}{x^2 + 3x - 10} - \frac{5}{x+5}$$

$$\frac{7}{(x+5)(x-2)} + \frac{-5}{(x+5)} \cdot \frac{(x-2)}{(x-2)}$$

$$\frac{7}{(x+5)(x-2)} + \frac{-5x+10}{(x+5)(x-2)} = \frac{-5x+17}{(x+5)(x-2)}$$

$\frac{-5x+17}{(x+5)(x-2)}$ (circled)

Adv. Algebra 2 – Concept Quiz

Form A

Name: *Key

Date: _____ Period: _____

21. Graphs of Rational Functions

a) Find the characteristics listed below of the function $f(x) = \frac{x^2 - 12x + 32}{x - 7}$. $\frac{(x-8)(x-4)}{x-7}$

a. Vertical Asymptote $x = 7$

b. End Behavior $y = x - 5$

c. x-intercept(s) $(8, 0)$ $(4, 0)$

d. y-intercept $(0, -\frac{32}{7})$

$$7 \overline{) \begin{array}{r} 1 \quad -12 \quad 32 \\ \quad 7 \quad -35 \\ \hline 1 \quad -5 \quad -3 \end{array}}$$

$$\boxed{x - 5 + \frac{-3}{x-7}}$$

b) As x gets larger and larger in the positive and negative direction, the graph of $g(x) = \frac{5x-19}{x-4}$ approaches the line $y = 5$. Explain why this is end behavior of $g(x)$.

22. Solving Rational Equations

a) Find all values of x that make the equation true.

$$\frac{5x}{x-5} - 2 = \frac{8}{x^2 - 5x}$$

$$\frac{5x}{x-5} + \frac{-2 \cdot (x-5)}{(x-5)} = \frac{8}{x(x-5)}$$

$$\frac{3x+10}{x-5} = \frac{8}{x(x-5)}$$

$$3x^2 + 10x = 8$$

$$3x^2 + 10x - 8 = 0$$

$$3x^2 + 12x - 2x - 8 = 0$$

$$3x(x+4) - 2(x+4) = 0$$

$$(x+4)(3x-2) = 0$$

$$\boxed{x = -4, \frac{2}{3}}$$

b) How can extraneous solutions arise in the process of solving an equation?

23. Multiply and Divide Rational Expressions

$$\frac{2x^2 - 13x + 15}{14x^3 - 21x^2} \div \frac{x^2 - 25}{14x^2 + 70x} = \frac{(2x-3)(x-5)}{\cancel{7} \cdot x \cdot \cancel{2} \cdot (2x-3)} \cdot \frac{7 \cdot 2 \cdot x(x+5)}{(x+5)(x-5)}$$

$$\frac{2x-3}{2x-3} \cdot \frac{7}{7} \cdot \frac{x}{x} \cdot \frac{(x-5)}{(x-5)} \cdot \frac{(x+5)}{(x+5)} \cdot \frac{2}{x}$$

$$\boxed{\frac{2}{x}}$$

24. Adding and Subtracting Rational Expressions

$$\frac{5x}{x+3} - \frac{3}{x^2 + 11x + 24} = \frac{5x}{x+3} \cdot \frac{(x+8)}{(x+8)} - \frac{3}{(x+8)(x+3)}$$

$$\frac{5x^2 + 40x}{(x+3)(x+8)} - \frac{3}{(x+8)(x+3)}$$

$$\boxed{\frac{5x+43}{(x+3)(x+8)}}$$

$$\frac{5x^2 + 40x - 3}{(x+8)(x+3)}$$